

# Continual Learning: On Machines that can Learn Continually

Official Open-Access Course @ University of Pisa, ContinualAI, AIDA

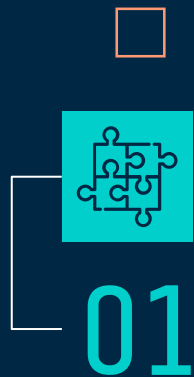
## Lecture 6: Methodologies [Part 2]

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The background is a dark blue gradient. It features several thin, vertical white lines of varying lengths scattered across the frame. Interspersed among these lines are small squares in three colors: light blue, orange, and teal. Some squares are solid, while others are outlined. The overall aesthetic is modern and minimalist.

# Regularization Strategies

# Early-Stopping, L1 & L2, Dropout

## Early Focus

- Study the impact of **activation functions**
- Study the impact of different **optimizers**
- **L2/L1 & Dropout** regularizations
- **Early-Stopping, mb-size** and **learning rate** impact

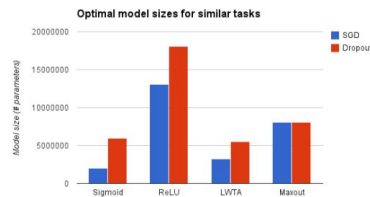


Figure 2. Optimal model size with and without dropout on the input reformatting tasks.

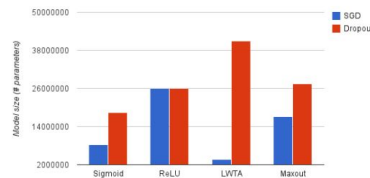


Figure 4. Optimal model size with and without dropout on the similar tasks experiment.

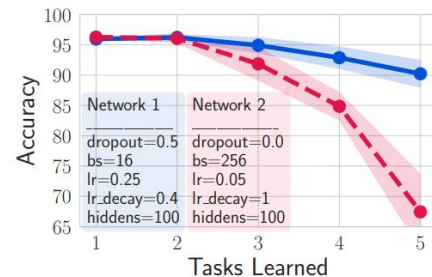


Figure 1: For the same architecture and dataset (Rotation MNIST) and only changing the training regime, the forgetting is reduced significantly at the cost of a relatively small accuracy drop on the current task. Refer to appendix C for details.

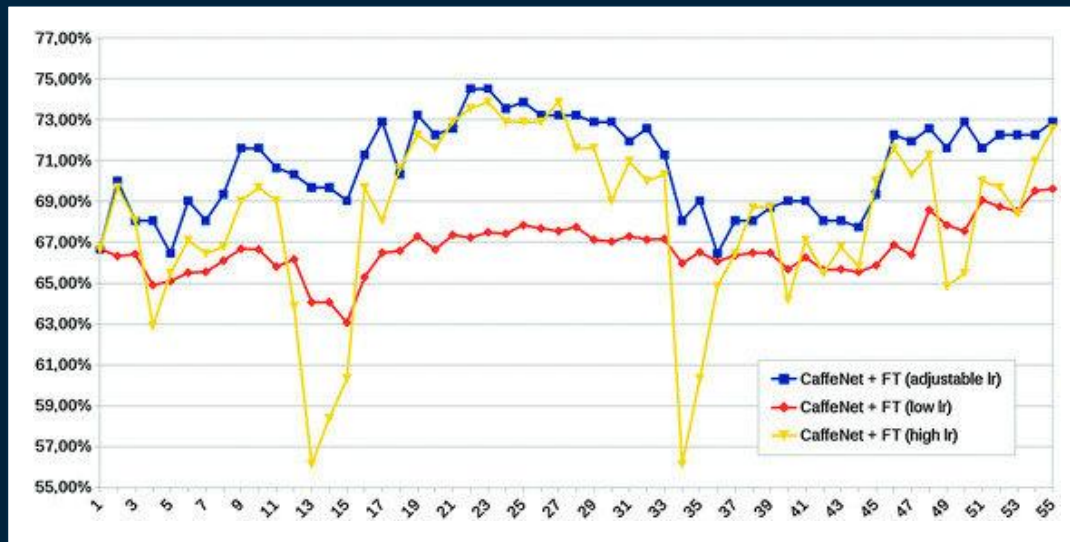
# Early-Stopping, L1 & L2, Dropout

## Big Brother Experiment

- 7 finalists who stayed in the house for **55 days**
- **Violet-Jones** to detect faces
- **Adjustable learning rate** based on thresholds



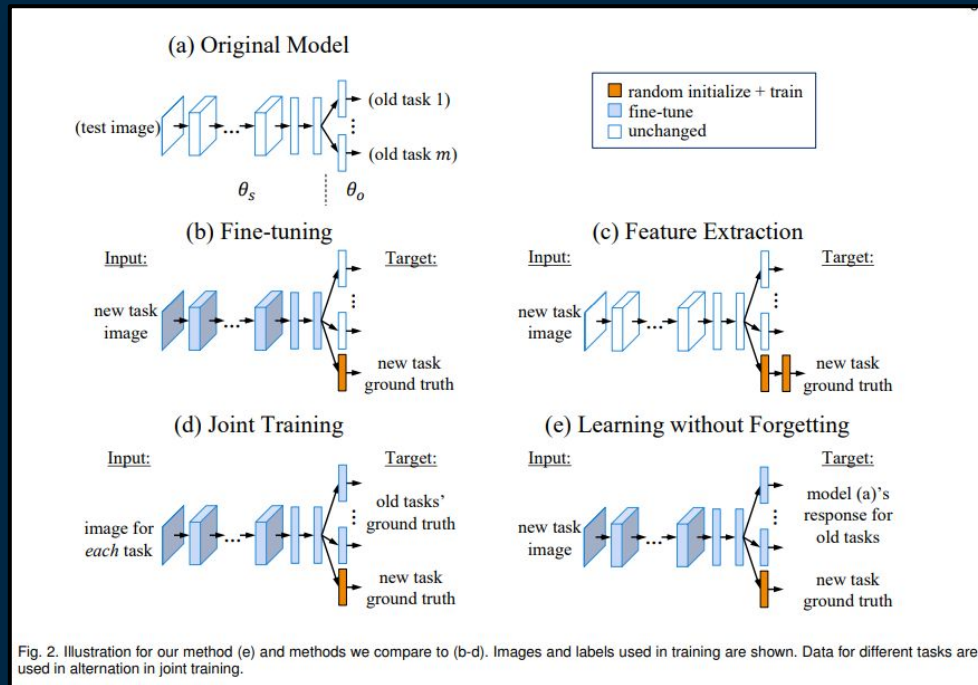
Fig. 2.  
Example images of the seven subjects contained in the SETB of the BigBrother Dataset.



# Learning Without Forgetting (LWF)

## Key Aspects

- Straightforward application of **Knowledge Distillation**
- Originally designed for **Task-Incremental settings** can be easily extended to others
- **Efficient single-head implementations** exist
- **Easy to implement** and commonly used



Learning without Forgetting, Li et al, TPAMI 2017

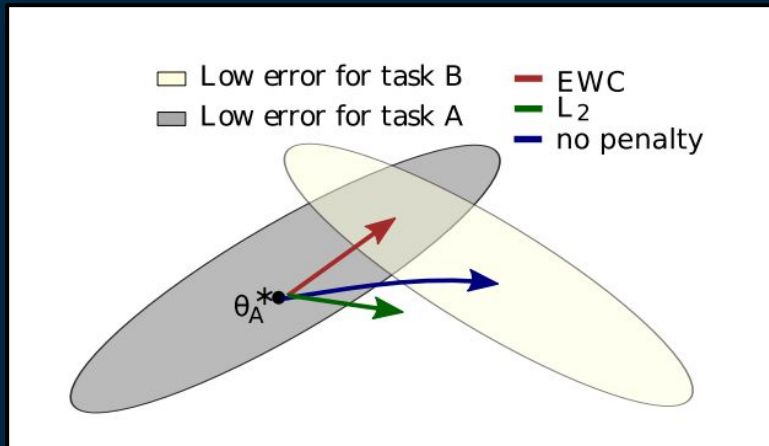
Distilling the knowledge in a neural network, Hinton et al, 2015.

Continuous Learning in Single-Incremental Tasks, Maltoni & Lomonaco, Neural Networks, 2019.

# Elastic Weights Consolidation (EWC)

## Key Aspects

- **Seminal work** that sparked new excitement and interest in *Deep Continual Learning*
- Interesting connection with more advanced computational neuroscience **memory consolidation theories**
- Many variations are possible: how to compute **parameters importance**? Do we need to maintain a **separate set of <optimal weights, importance values>** for each experience?



$$\mathcal{L}(\theta) = \mathcal{L}_B(\theta) + \sum_i \frac{\lambda}{2} F_i (\theta_i - \theta_{A,i}^*)^2$$

# Synaptic Intelligence (SI)

## Key Aspects

- A **simple yet effective** way of computing weights importances
- Main idea: “a parameter **importance is proportional to its contribution to the loss decrease** over time”
- Even in this case **efficient online implementation exists**
- Hyper-parameters may be **difficult to calibrate**

$$L(\theta(t) + \delta(t)) - L(\theta(t)) \approx \sum_k g_k(t) \delta_k(t), \quad (1)$$

$$\int_C g(\theta(t)) d\theta = \int_{t_0}^{t_1} g(\theta(t)) \cdot \theta'(t) dt. \quad (2)$$

$$\begin{aligned} \int_{t^{\mu-1}}^{t^\mu} g(\theta(t)) \cdot \theta'(t) dt &= \sum_k \int_{t^{\mu-1}}^{t^\mu} g_k(\theta(t)) \theta'_k(t) dt \\ &\equiv - \sum_k \omega_k^\mu. \end{aligned} \quad (3)$$

$$\tilde{L}_\mu = L_\mu + c \underbrace{\sum_k \Omega_k^\mu \left( \tilde{\theta}_k - \theta_k \right)^2}_{\text{surrogate loss}} \quad (4)$$

$$\Omega_k^\mu = \sum_{\nu < \mu} \frac{\omega_k^\nu}{(\Delta_k^\nu)^2 + \xi}. \quad (5)$$



# CL with Hypernetworks

## Key Aspects

- Main idea: *let's learn how to generate network weights*
- It may be seen as a form of **neurogenesis regulation**
- **Underlying hypothesis:** learning in this “compressed” space is less subject to forgetting
- **Difficult to scale** on higher-dimensional problems and without tasks labels

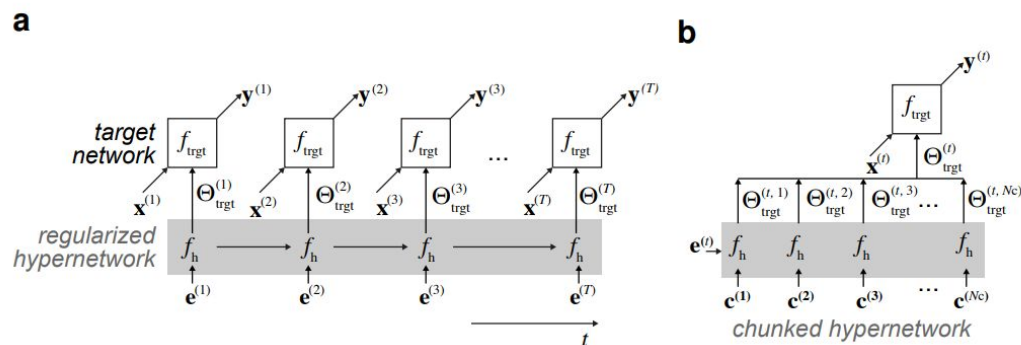


Figure 1: **Task-conditioned hypernetworks for continual learning.** (a) Commonly, the parameters of a neural network are directly adjusted from data to solve a task. Here, a weight generator termed *hypernetwork* is learned instead. Hypernetworks map embedding vectors to weights, which parameterize a target neural network. In a continual learning scenario, a set of task-specific embeddings is learned via backpropagation. Embedding vectors provide task-dependent context and bias the hypernetwork to particular solutions. (b) A smaller, chunked hypernetwork can be used iteratively, producing a chunk of target network weights at a time (e.g., one layer at a time). Chunked hypernetworks can achieve model compression: the effective number of trainable parameters can be smaller than the number of target network weights.

# Summary & Next Steps

- Quite **elegant formulation** (mostly changing the loss function, adding regularization terms)
- Towards a **more principled definition of continual optimization**
- **Especially effective in Domain-Incremental** scenarios
- Better investigation in the gradient dynamics while learning may be useful
- **Plug & play orthogonal regularization terms** may be interesting to study
- We expect **significant advances** in this area in the years to come

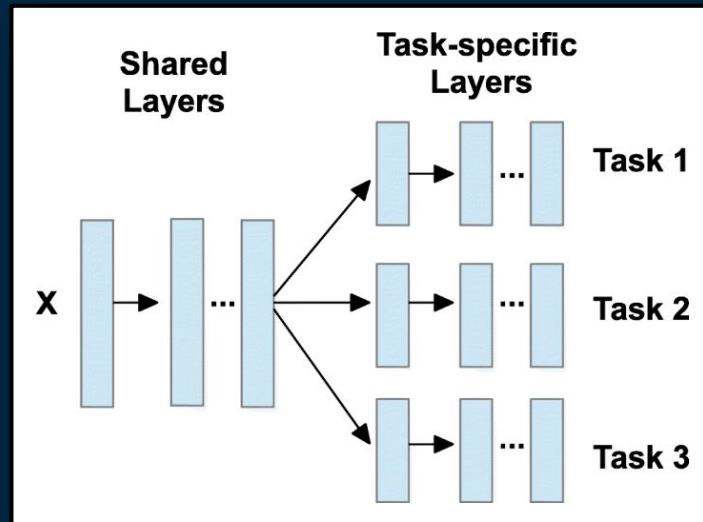
The background is a dark blue gradient. It is decorated with various geometric elements: thin white vertical lines of varying lengths, small squares in teal, orange, and pink, and larger squares in teal and orange. The text 'Architectural Strategies' is centered in the middle of the image.

# Architectural Strategies

# Multi-Head Architectures

## Key Elements

- Great to **specialize behaviours if the notion of task is explicit**
- It clearly separate **shared parameters** with **private parameters**
- It may be constructed **“internally”** by the model when a significant “shift” is detected
- **A new head for each experience**: quite inefficient and possibly ineffective



# Copy Weights with Re-Init (CWR)

## Key Aspects

- Developed for the **fully connected linear classifier** (may be extended to multiple layers)
- Dual memory system approach**: one for better plasticity, one for memory consolidation
- Very simple and efficient, yet effective solution **agnostic to the experience content (NI, NC, NIC) and specific scenario**

**Algorithm 1** CWR\* pseudocode:  $\bar{\Theta}$  are the class-shared parameters of the representation layers; the notation  $cw[j]$  /  $tw[j]$  is used to denote the groups of consolidated / temporary weights corresponding to class  $j$ . Note that this version continues to work under NC, which is seen here a special case of NIC; in fact, since in NC the classes in the current batch were never encountered before, the step at line 7 loads 0 values for classes in  $B_i$  because  $cw_j$  were initialized to 0 and in the consolidation step (line 13)  $wpast_j$  values are always 0.

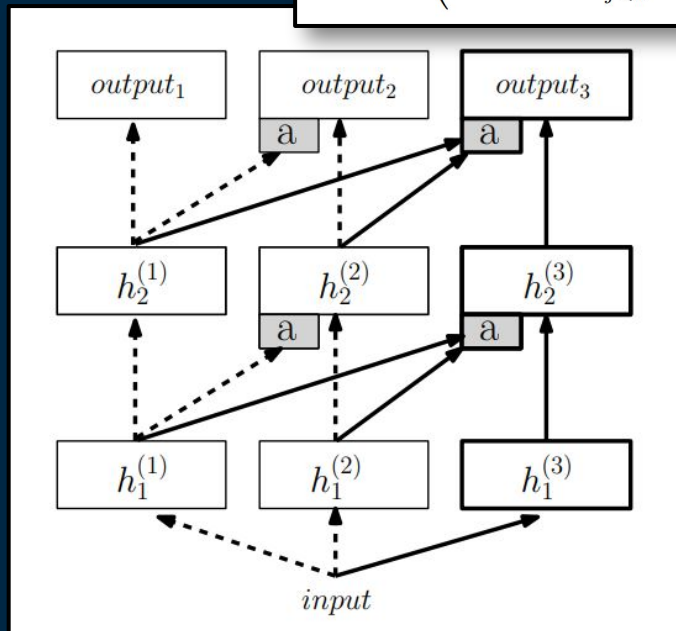
```
1: procedure CWR*
2:    $cw = 0$ 
3:    $past = 0$ 
4:   init  $\bar{\Theta}$  random or from pre-trained model (e.g. on ImageNet)
5:   for each training batch  $B_i$ :
6:     expand output layer with neurons for the new classes in  $B_i$ 
       never seen before
7:      $tw[j] = \begin{cases} cw[j], & \text{if class } j \text{ in } B_i \\ 0, & \text{otherwise} \end{cases}$ 
8:     train the model with SGD on the  $s_i$  classes of  $B_i$ :
9:       if  $B_i = B_1$  learn both  $\bar{\Theta}$  and  $tw$ 
10:      else learn  $tw$  while keeping  $\bar{\Theta}$  fixed
11:      for each class  $j$  in  $B_i$ :
12:         $wpast_j = \sqrt{\frac{past_j}{cur_j}}$ , where  $cur_j$  is the number of patterns
          of class  $j$  in  $B_i$ 
13:         $cw[j] = \frac{cw[j] \cdot wpast_j + (tw[j] - avg(tw))}{wpast_j + 1}$ 
14:         $past_j = past_j + cur_j$ 
15:      test the model by using  $\bar{\Theta}$  and  $cw$ 
```

# Progressive Neural Networks (PNNs)

## Key Aspects

- Main **focus on forward transfer** and re-use of previously acquired representational power
- **Previous “columns” are frozen** inhibiting backward knowledge transfer
- Quite inefficient: **significant grow in the parameter space**, very difficult to scale on longer sequences of experiences
- **Adapters + pruning** can be used to tame complexity

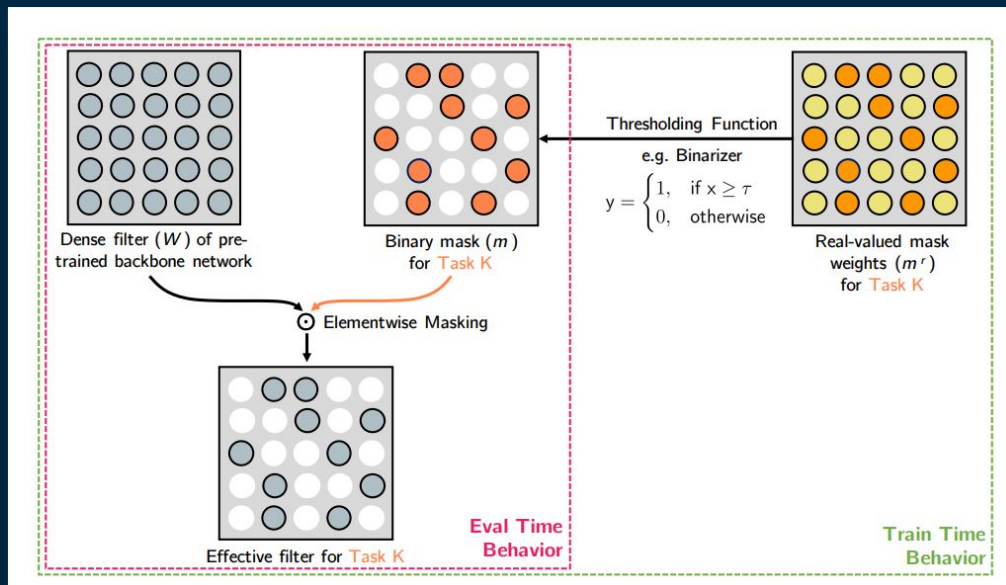
$$h_i^{(k)} = f \left( W_i^{(k)} h_{i-1}^{(k)} + \sum_{j < k} U_i^{(k:j)} h_{i-1}^{(j)} \right)$$



# Weights Mask (Piggyback)

## Key Aspects

- Starting from a **pre-trained model** (backbone)
- Adding a **mask for each weight**, train float then binarize
- This achieves **zero-forgetting**, but no knowledge transfer
- It is quite efficient, and **handful of KBs per experience / task**, but it needs task labels



# Hard Attention to the Task (HAT)

## Key Aspects

- Similar idea as Piggyback: use **hard attention masks** for each task
- The **mask is on the neurons not weights** (as “**inhibitory synapses**”), gradients masks can be created based on them
- Some form of forward transfer exist in the concept of “**cumulative attention**” and no pre-train model is necessary
- **Good accuracy-effectiveness trade-off** (binary vs real attention masks)
- Subject to the same limitations as Piggyback as for the **task labels availability**

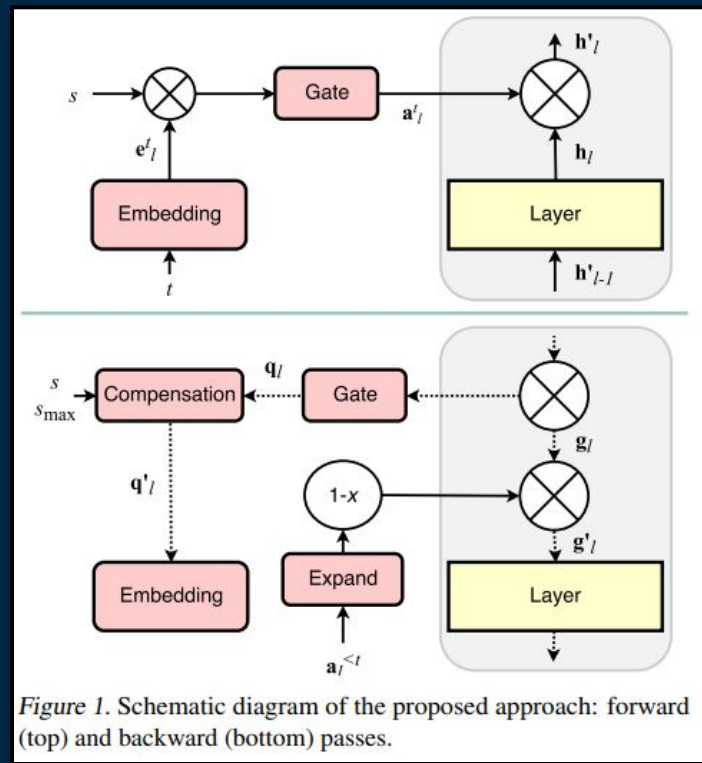


Figure 1. Schematic diagram of the proposed approach: forward (top) and backward (bottom) passes.



# Supermasks in Superimposition

## Key Aspects

- **Good binary masks** that applied to **random weights** exist
- **Random weights can be generated** on the fly based on random seed
- They can be used in **superimposition**

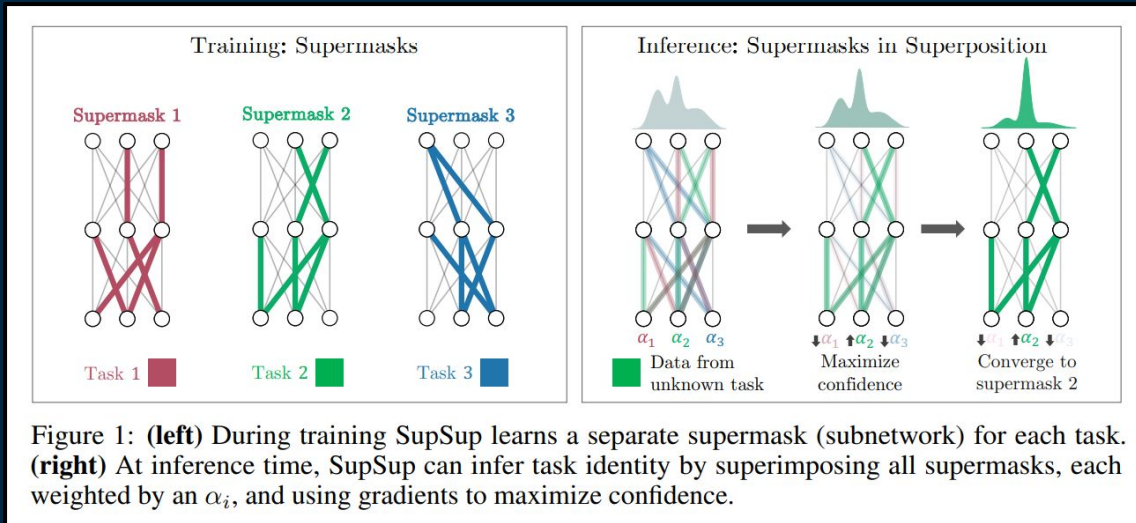


Figure 1: **(left)** During training SupSup learns a separate supermask (subnetwork) for each task. **(right)** At inference time, SupSup can infer task identity by superimposing all supermasks, each weighted by an  $\alpha_i$ , and using gradients to maximize confidence.

# Summary & Next Steps

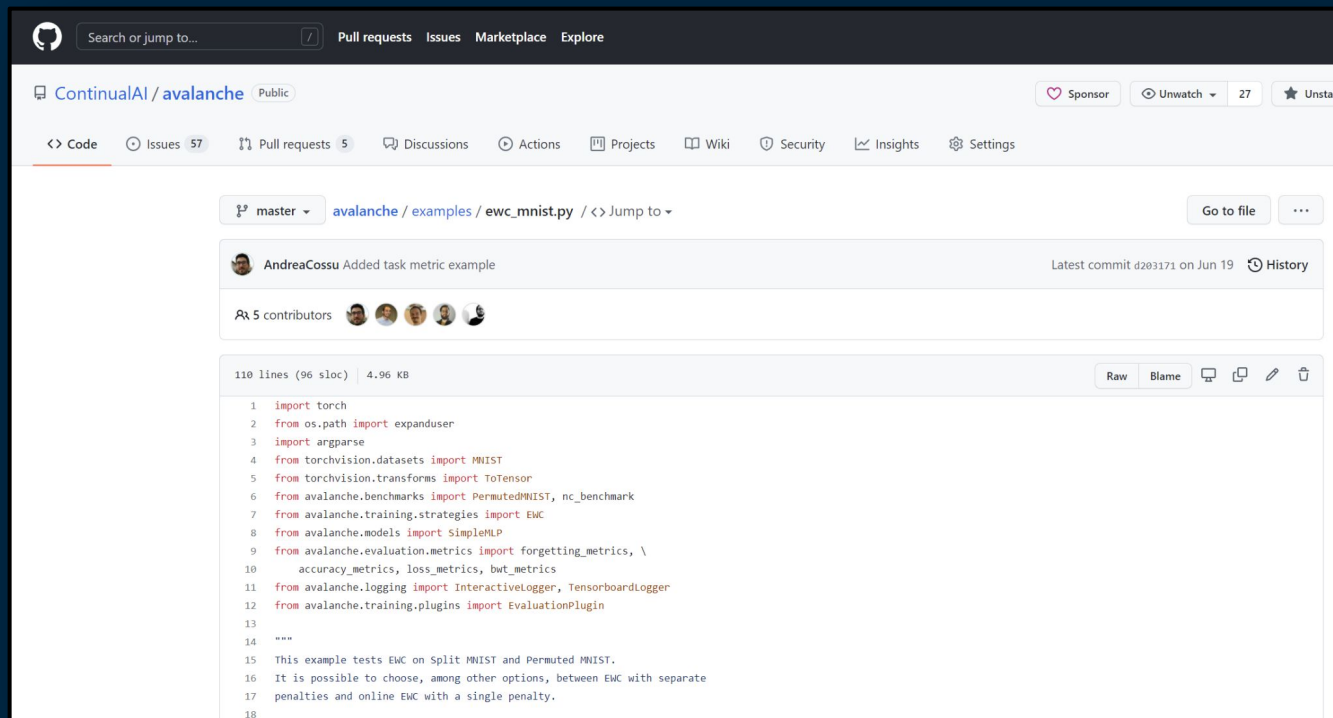
- Architectural methods may be **quite effective in terms of performance metrics** and reducing forgetting (knowledge preserving)
- **Difficult to perform efficient knowledge transfer** and parameter sharing
- Often involve **constant growing in the parameter space**
- The **often leverage task-specific supervised signals**
- Interesting **link** with **structural plasticity** in biological learning systems
- More **flexible and dynamic architecture re-arrangements** based on available resources may be an interesting future research direction

The background is a dark blue gradient. It is decorated with various geometric elements: thin white vertical lines of varying lengths, small squares in teal, orange, and pink, and larger squares in teal and orange. The text 'Avalanche' is in white, and 'Implementation' is in orange. A small white square is positioned below the 'v' in 'Avalanche'.

# Avalanche Implementation

# Avalanche EWC, LWF & CWR Implementation

**Demo Session!**



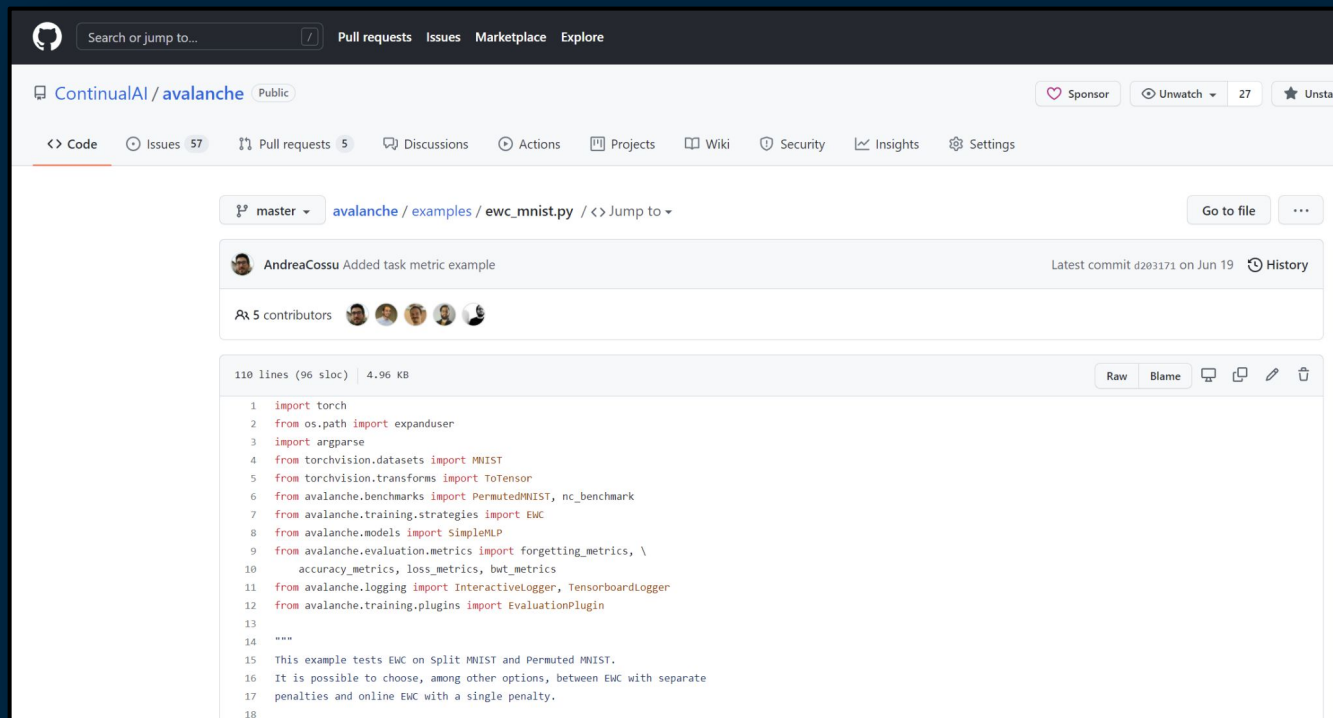
The screenshot shows the GitHub interface for the repository `ContinualAI/avalanche`. The file `avalanche/examples/ewc_mnist.py` is selected, showing its commit history and contributors. The code content is displayed below, starting with imports for `torch`, `os.path`, `argparse`, `torchvision`, and `avalanche` modules. The code includes a docstring describing the example's purpose: testing EWC on Split MNIST and Permuted MNIST, and comparing different EWC implementations.

```
110 lines (96 sloc) | 4.96 KB
Raw Blame

1 import torch
2 from os.path import expanduser
3 import argparse
4 from torchvision.datasets import MNIST
5 from torchvision.transforms import Totensor
6 from avalanche.benchmarks import PermutedMNIST, nc_benchmark
7 from avalanche.training.strategies import EWC
8 from avalanche.models import SimpleMLP
9 from avalanche.evaluation.metrics import forgetting_metrics, \
10     accuracy_metrics, loss_metrics, bwt_metrics
11 from avalanche.logging import InteractiveLogger, TensorboardLogger
12 from avalanche.training.plugins import EvaluationPlugin
13
14 """
15 This example tests EWC on Split MNIST and Permuted MNIST.
16 It is possible to choose, among other options, between EWC with separate
17 penalties and online EWC with a single penalty.
18
```

# Your Turn: Regularization Strategies in Class-Incremental Scenarios

**Hands-on Session!**



The screenshot shows the GitHub interface for the repository `ContinualAI/avalanche`. The file `examples/ewc_mnist.py` is selected, showing its commit history and contributors. The code is displayed in a light blue editor with line numbers. The file contains imports for `torch`, `os.path`, `argparse`, `torchvision`, `avalanche`, and `logging`. It also includes a docstring describing the example.

```
1 import torch
2 from os.path import expanduser
3 import argparse
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# Next:

## Methodologies [Part 3], Applications & Tools

Do you have any questions?

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# THANKS



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